

Speech Analysis by AFD

by

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Approved by \_\_\_\_\_  
Supervisor

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by Sifan Wu

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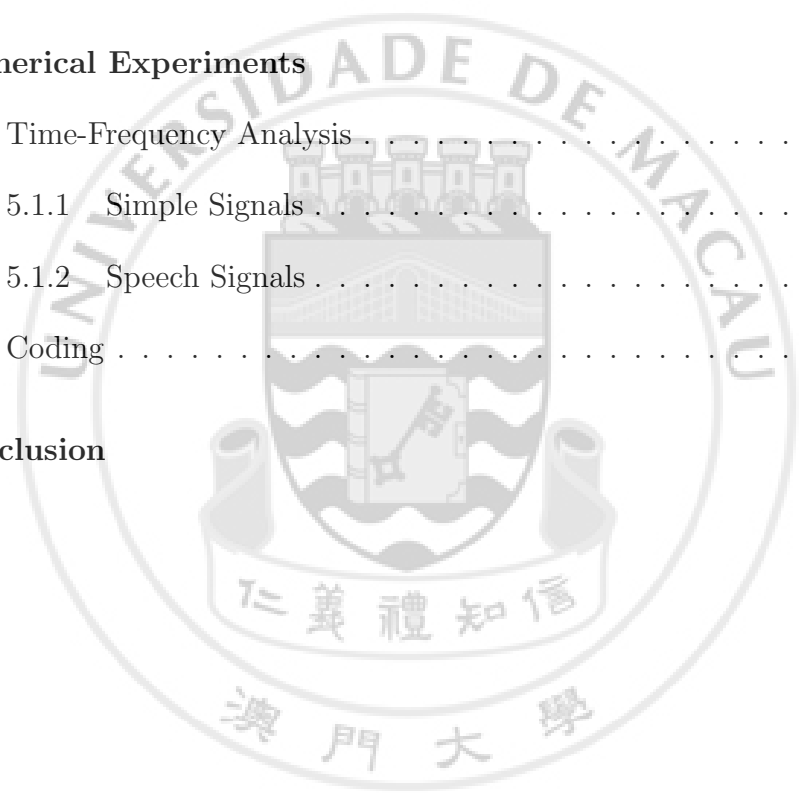
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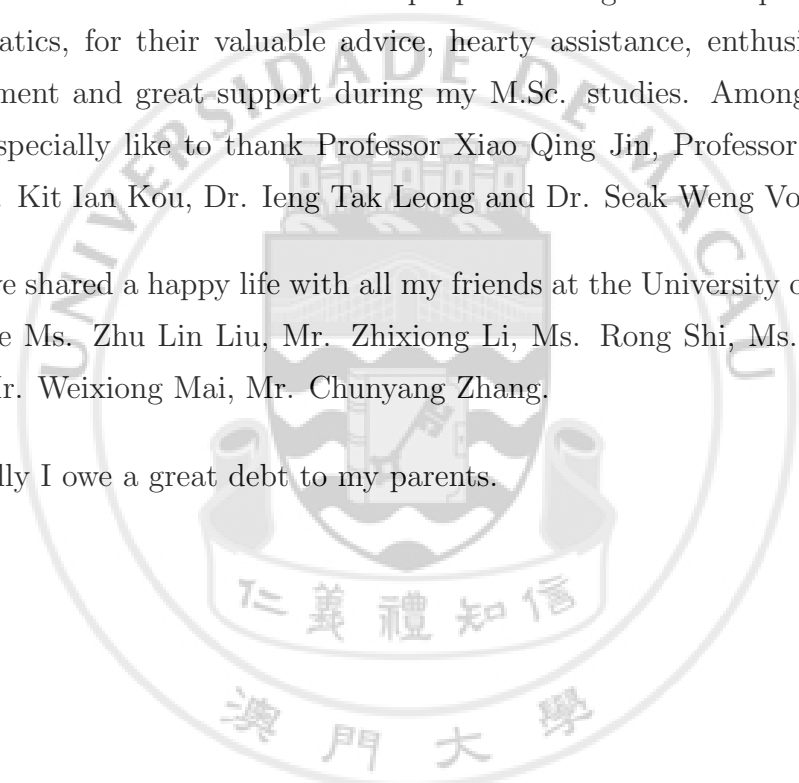
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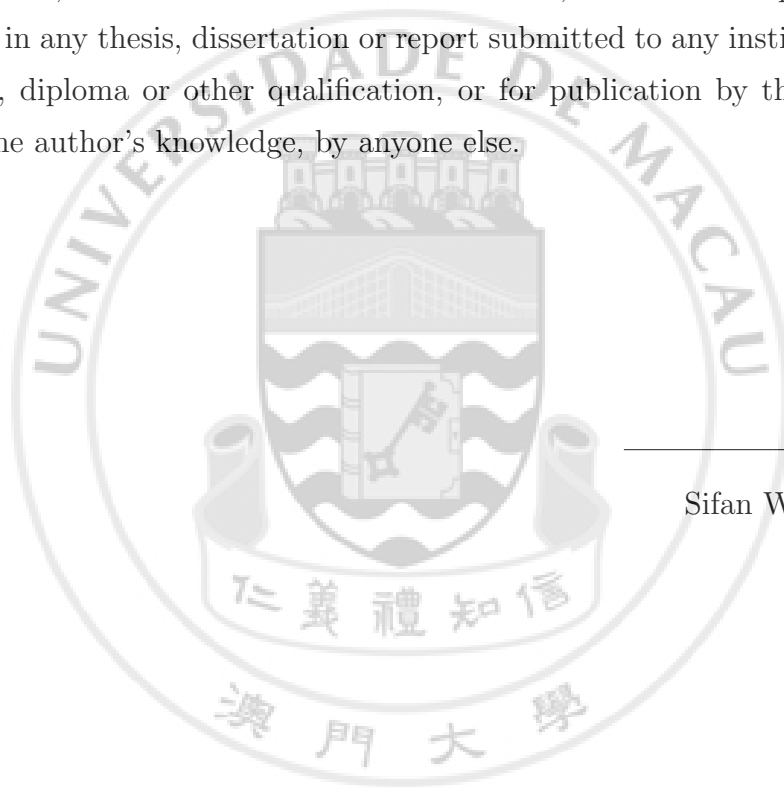
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## DECLARATION

The author declares that this thesis represents his own work with Professor Tao Qian, the author's supervisor. All the work is done under the supervision of Professor Qian during the period 2011-2012 for the degree of Master of Science in Mathematics at the University of Macau. The results in this thesis, unless otherwise stated or indicated, have not been previously included in any thesis, dissertation or report submitted to any institution for a degree, diploma or other qualification, or for publication by the author, and to the author's knowledge, by anyone else.



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