

**Study of Progressive LOD Techniques on Static and
Dynamic Models in Digital Geometry Processing**

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