

**The Linear Canonical Transform and Generalized Hilbert
Transform with Applications in Signal Processing**

by

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