

**UNIVERSITY OF MACAU**

**FACULTY OF BUSINESS ADMINISTRATION**

A MULTIVARIATE CONTROL CHART FOR  
MONITORING UNIVARIATE PROCESSES

Tian Wen Jing

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