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**Some Properties of T. Chan's Preconditioner and Applications in
Numerical Differential Equations**

by

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