

**EARTHQUAKE-INDUCED RANDOM  
VIBRATION ANALYSIS OF CABLE-STAYED  
BRIDGE WITH FINITE STRIP ELEMENTS**

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