

**Analysis on GMRES Convergence and
Some Results on Spectral Properties
of Preconditioned Matrices**

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